

ELEG5481 Signal Processing Optimization Techniques

Tutorial 7

Mar. 17, 2013

Q1. Use CVX to solve the following problem

$$\begin{aligned} \min_{x,y} \quad & c^T x \\ \text{s.t.} \quad & x = Ay \\ & l_y \leq y \leq u_y, \\ & l_x \leq x \leq u_x, \\ & x \in \mathbf{R}^m, y \in \mathbf{R}^n, \end{aligned}$$

where $A \in \mathbf{R}^{m \times n}$, $l_y, u_y \in \mathbf{R}^n$, $l_x, u_x \in \mathbf{R}^m$, and $c \in \mathbf{R}^m$ are given data.

Q2. Use CVX to solve the following problem

$$\begin{aligned} \min_{x,y} \quad & x^T Q_0 x \\ \text{s.t.} \quad & x = Ay \\ & x^T Q_i x \leq b_i, i = 1, \dots, p \\ & y \leq u, \\ & x \in \mathbf{R}^m, y \in \mathbf{R}^n, \end{aligned}$$

where $A \in \mathbf{R}^{m \times n}$, $Q_i \in \mathbf{S}_+^m$, $b \in \mathbf{R}^p$, and $u \in \mathbf{R}^n$ are given data.

Q3. Use CVX to solve the following problem

$$\begin{aligned} \min_X \quad & \text{tr}CX \\ \text{s.t.} \quad & X \in \mathbf{H}_+^n, \\ & \text{tr}A_i X \leq b_i, i = 1, \dots, p, \\ & \text{tr}E_j X = f_j, j = 1, \dots, q, \end{aligned}$$

where the given data are $C \in \mathbf{H}^n$, $A_i, E_j \in \mathbf{H}^n$, $b_i \geq 0$, and $f_j \geq 0$. Here, \mathbf{H}_+^n denotes the set of Hermitian semidefinite matrix.